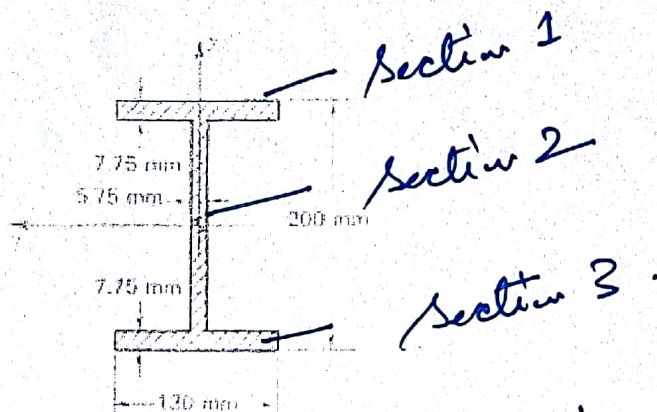


Name: _____ Roll no. _____

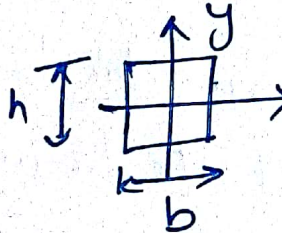
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AS 2010: Basic strength of materials. Quiz 10

1. Calculate the second moment of area, I_{zz} for the section illustrated.



Given c/s is symmetric about axis, zz

 ; $I_{xx} = \frac{bh^3}{12}$; $I_{yy} = \frac{hb^3}{12}$

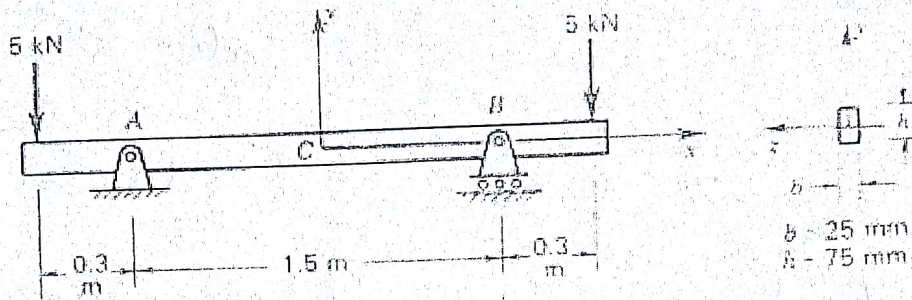
So; use the parallel axis theorem to find out the, I_{zz}

$$I_{zz} = 2 \left[\frac{130 \times 7.75^3}{12} + 130 \times 7.75 \times \left(100 - \frac{7.75}{2}\right)^2 \right] + \left[\frac{5.75 \times (200 - 2 \times 7.75)^3}{12} \right]$$

$$= 2 \times 18.6287 \times 10^6 \text{ mm}^4 + 3.00937 \times 10^6 \text{ mm}^4$$

$$I_{zz} = 21.638 \times 10^6 \text{ mm}^4$$

2. A steel beam ($E = 200 \text{ GPa}$) is pinned at supports A and B and loaded as shown. Determine (i) the bending moment at the mid-point between the two supports, and (ii) the maximum tensile stress developed at that section.



$$\sum F_y = 0; \quad V_A + V_B = 10 \text{ kN}$$

$$V_A = V_B = 5 \text{ kN}; \quad \therefore \text{due to symmetric loading}$$

Moment @ point C, i.e. - mid point of the beam

$$M_C = 5 \times \left(0.3 + \frac{1.5}{2}\right) - 5 \times \frac{1.5}{2}$$

(i)

$$M_C = 1.5 \text{ kN-m}$$

(ii)

From Bending equation; $\frac{M}{I} = \frac{\sigma}{y} = \frac{E}{R}$

$$\sigma_{\max} = \frac{M}{I} \times y_{\max}; \quad y_{\max} = \pm h/2$$

$$= \frac{1.5 \times 10^3 \times \left(\frac{75 \times 10^{-3}}{2}\right)}{I}; \quad \text{where, } I = \frac{bh^3}{12}$$

$$I = 8.789 \times 10^{-7}$$

$$= \frac{25 \times 75^3}{12}$$

$$= 8.789 \times 10^{-7} \text{ m}^4$$

$$\sigma_{\max} = 64 \text{ MPa}$$

for max compressive stress, take $y_{\max} = (-h/2)$.